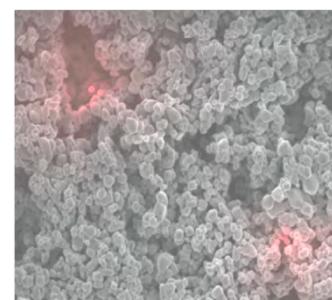
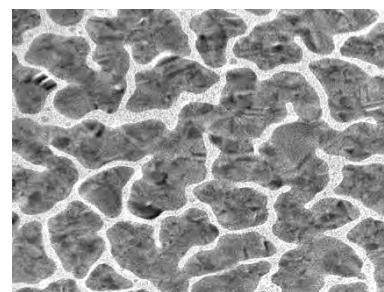


# Probing confined photons in nanoscale disordered media from inside

Rémi Carminati

Institut Langevin, ESPCI ParisTech, CNRS  
Paris, France

*remi.carminati@espci.fr*



# People involved

## "Physical optics and wave theory" group (ESPCI)



Romain PI ERRAT  
CNRS researcher



Etienne CASTANI E  
PhD student



Alexandre CAZE  
PhD student

## Collaborations



Yannick DE WILDE  
(ESPCI)



Valentina  
KRACHMALNI COFF  
Post-doc



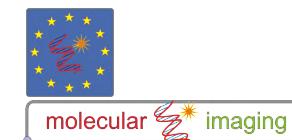
Mohamed ELABED  
Associate researcher



Rémi VINCENT  
Post-doc  
(until July 2011)

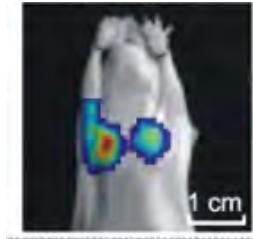
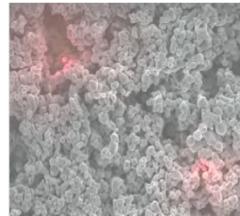


Riccardo SAPI ENZA  
Niek van HULST  
(I CFO Barcelona, Spain)

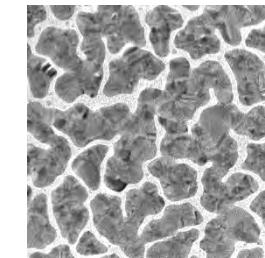


# Coupling spontaneous emission with disorder

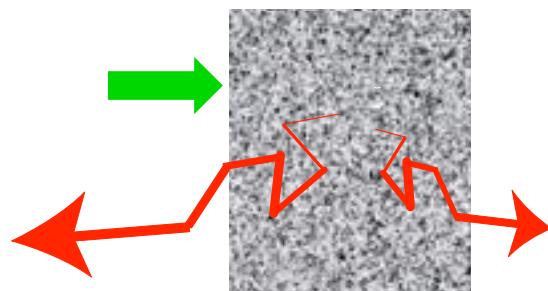
Fluorescence of nanosources  
in disordered media  
(photonic materials, imaging)



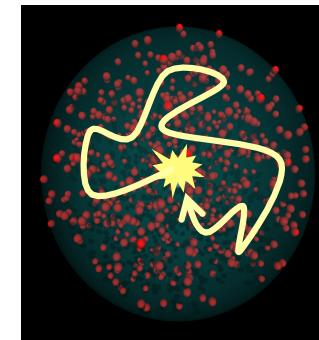
Nanophotonics - Light concentration on  
the nanoscale ("hot spots")



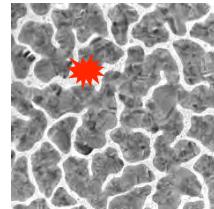
Novel light sources  
(e.g. random lasers)



Fundamental studies of light  
transport in scattering media  
(e.g. probing Anderson localization)



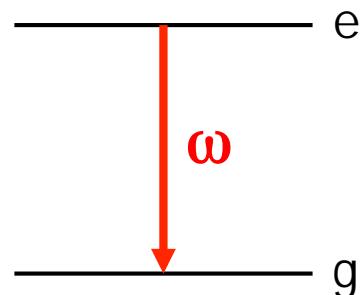
# Outline



Spontaneous emission and plasmonics:  
From nano-antennas to disordered systems

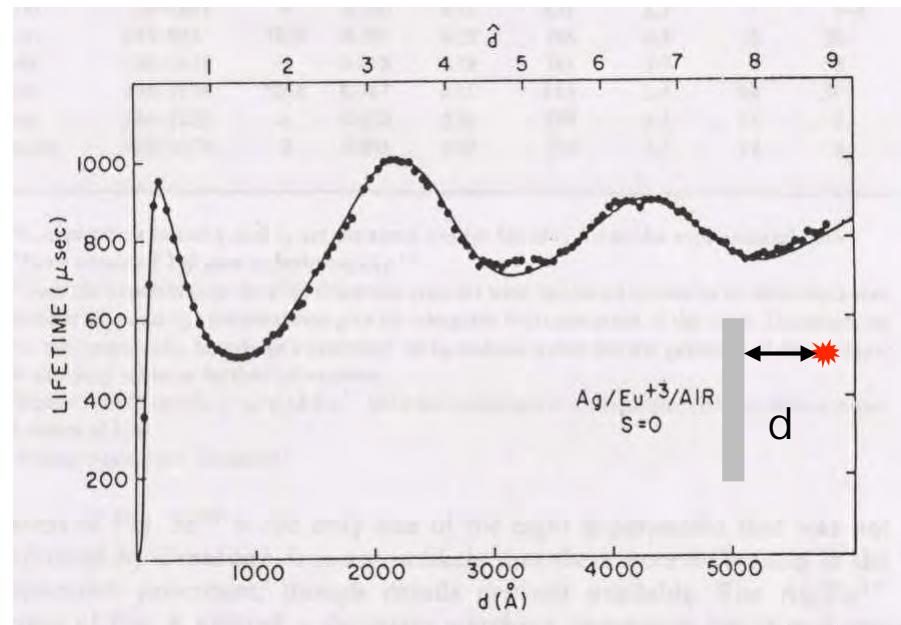
Probing near-field interactions in volume  
disordered systems

# Spontaneous decay rate



Probability of being excited at time  $t$        $P(t) \propto \exp(-\Gamma t)$

Lifetime of excited state       $\tau = 1/\Gamma$



Drexhage (1970)  
Chance, Prock, Silbey (1978)

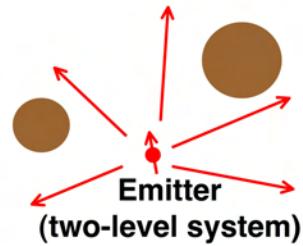
- The spontaneous decay rate depends on the environment

- Perturbation theory:

$$\Gamma = \frac{2}{\hbar} \mu_0 \omega_{ge}^2 |\mathbf{p}_{ge}|^2 \operatorname{Im} [\mathbf{u} \cdot \mathbf{G}(\mathbf{r}_0, \mathbf{r}_0, \omega_{ge}) \mathbf{u}]$$

Wiley and Sipe, Phys. Rev. A 30, 1185 (1984)

# Decay rate and LDOS



$$\Gamma = \frac{2}{\hbar} \mu_0 \omega^2 |\mathbf{p}_{ge}|^2 \text{Im}[\mathbf{u} \cdot \mathbf{G}(\mathbf{r}_0, \mathbf{r}_0, \omega) \mathbf{u}]$$

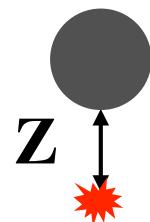
is also very often written as  
(Fermi golden rule)

$$\Gamma = \frac{\pi \omega}{3 \epsilon_0 \hbar} |\mathbf{p}_{ge}|^2 \rho_{\mathbf{u}}(\mathbf{r}_0, \omega)$$

Local Density  
of States (LDOS)

$$\frac{\Gamma}{\Gamma_0} = \text{change in the LDOS}$$

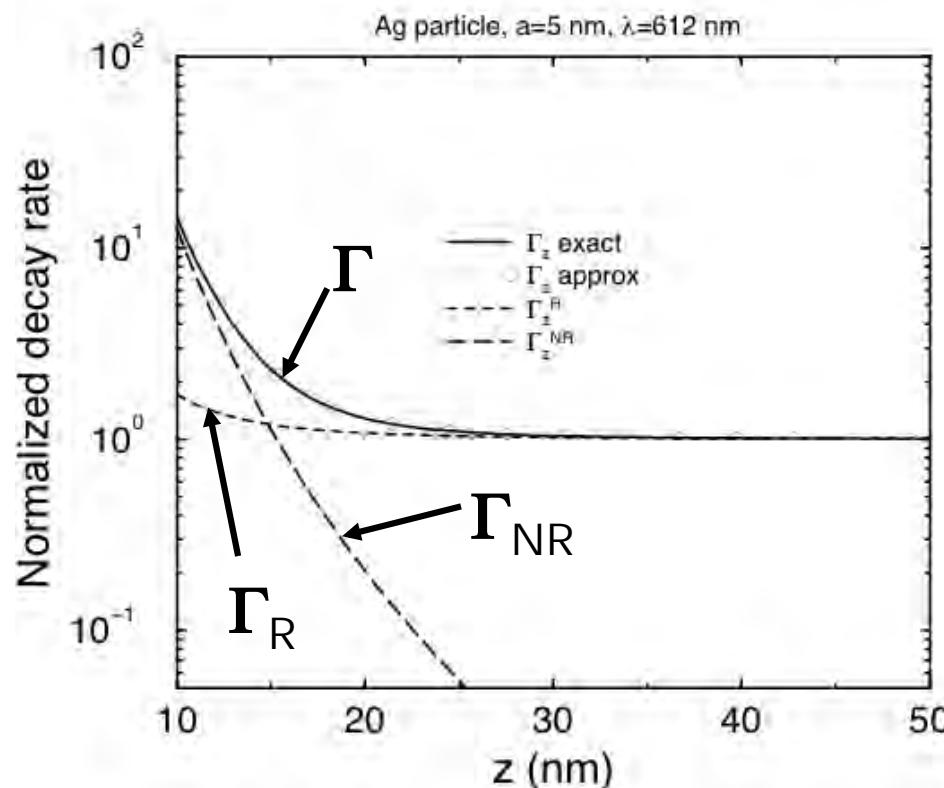
# Interaction with a single nanoparticle



Silver nanoparticle  
Diameter 10 nm

$$\Gamma = \Gamma_R + \Gamma_{NR}$$

Photon emission      Absorption

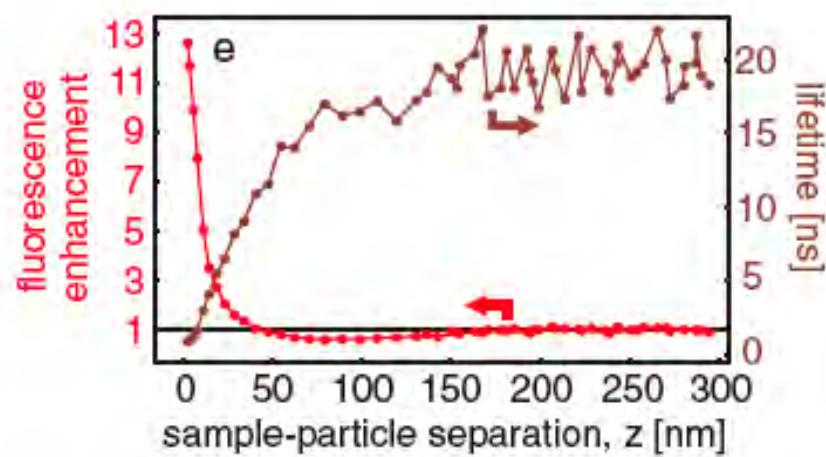
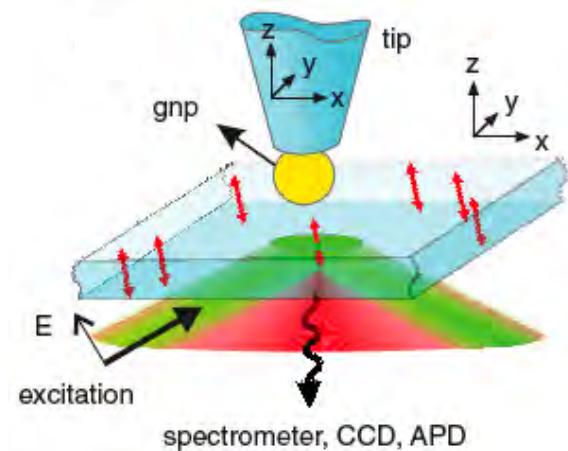


Leading contributions  
at short distance

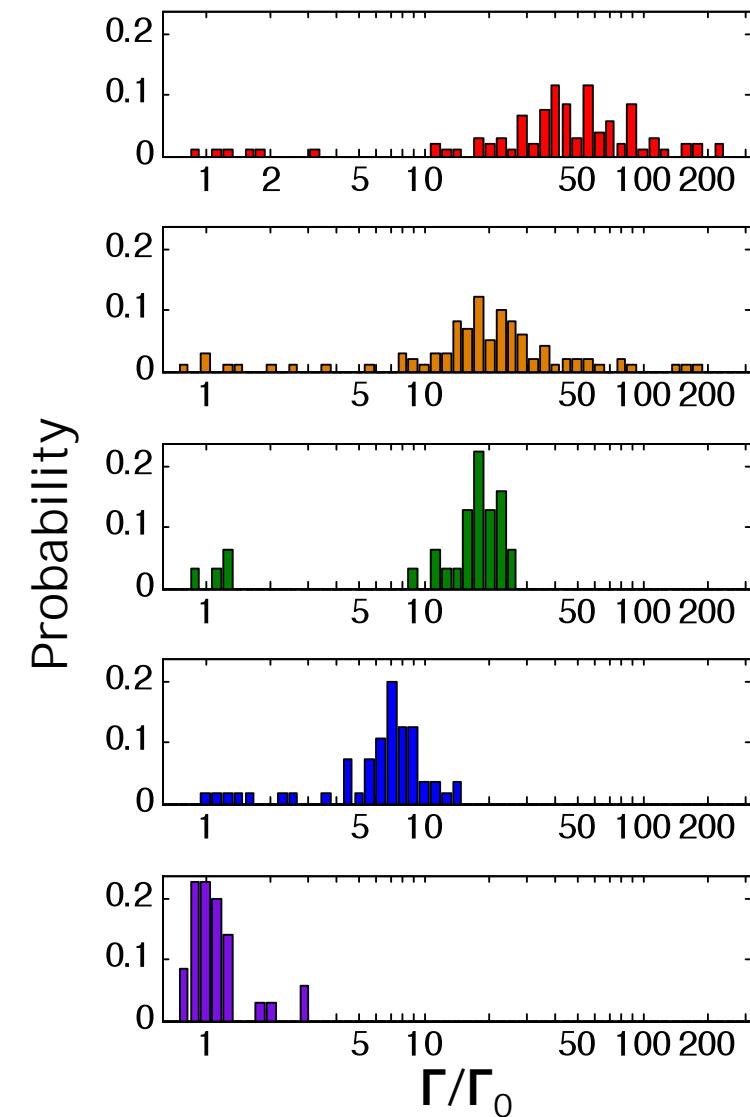
$$\Gamma_R \propto \frac{1}{(k z)^3}$$

$$\Gamma_{NR} \propto \frac{1}{(k z)^6}$$

# Nanoscale controlled experiments on single emitter



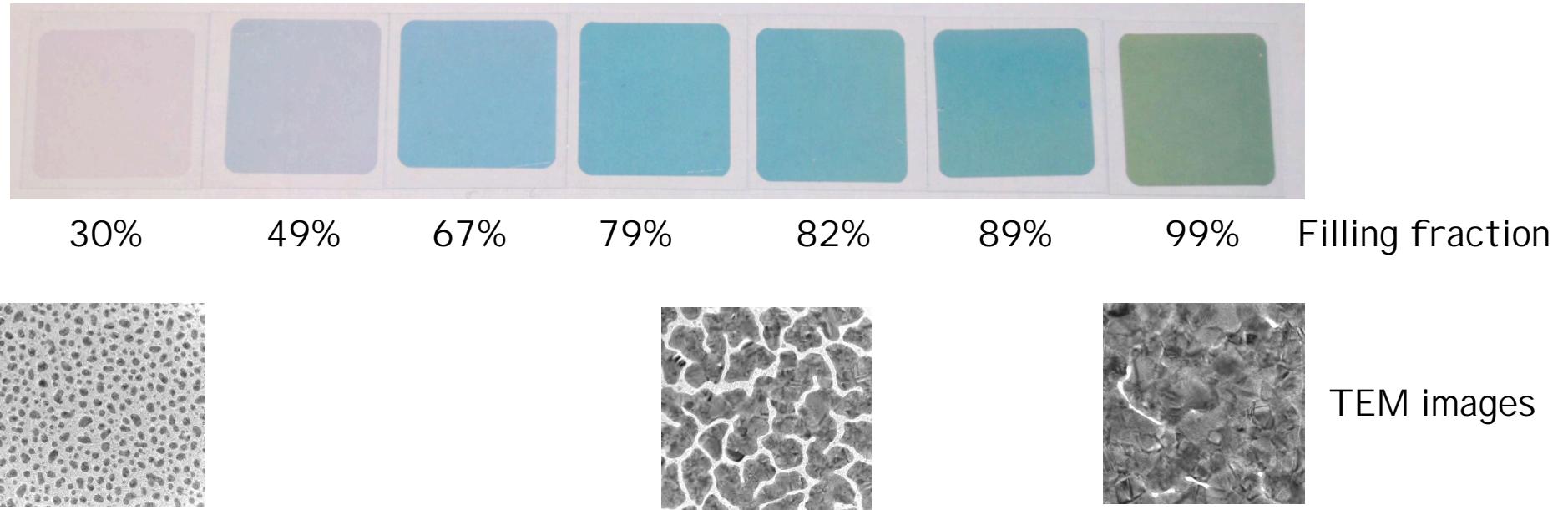
S. Kühn *et al.*, PRL 97, 017402 (2006)



M. Busson, S. Bidault *et al.* (2011)

# Peculiar optical properties of disordered metal films

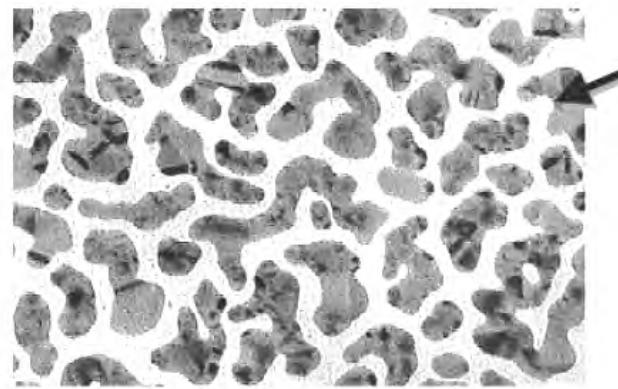
Semi-continuous gold films on a glass substrate



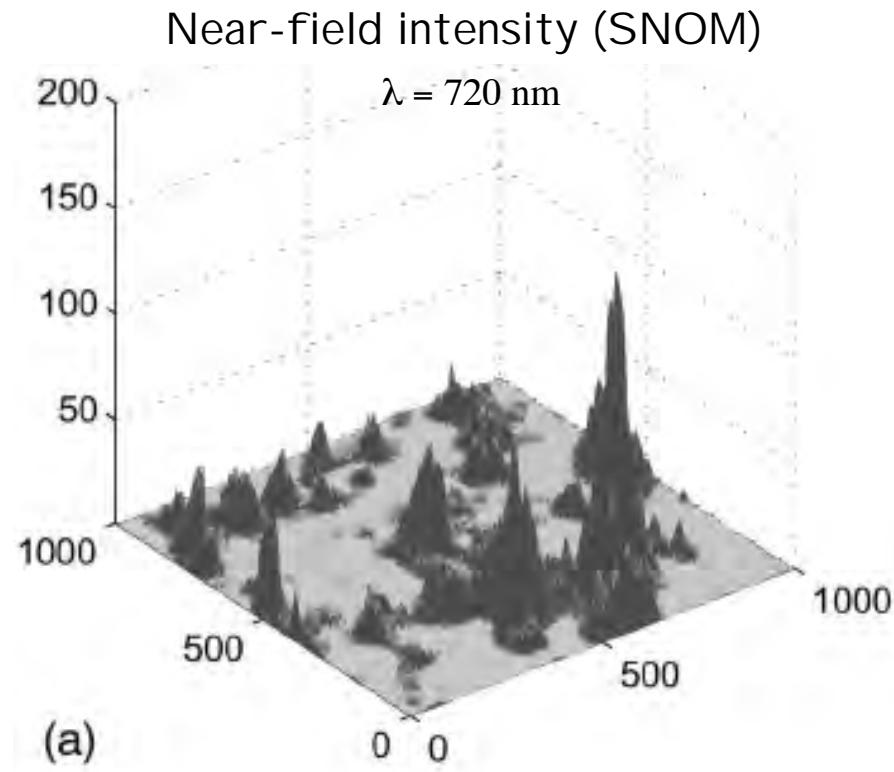
P. Gadenne *et al.*, J. Appl. Phys. 66, 3019 (1989)

V.M. Shalaev, *Nonlinear Optics of Random Media* (Springer, 2000)

# Near-field intensity distribution - « hot spots »

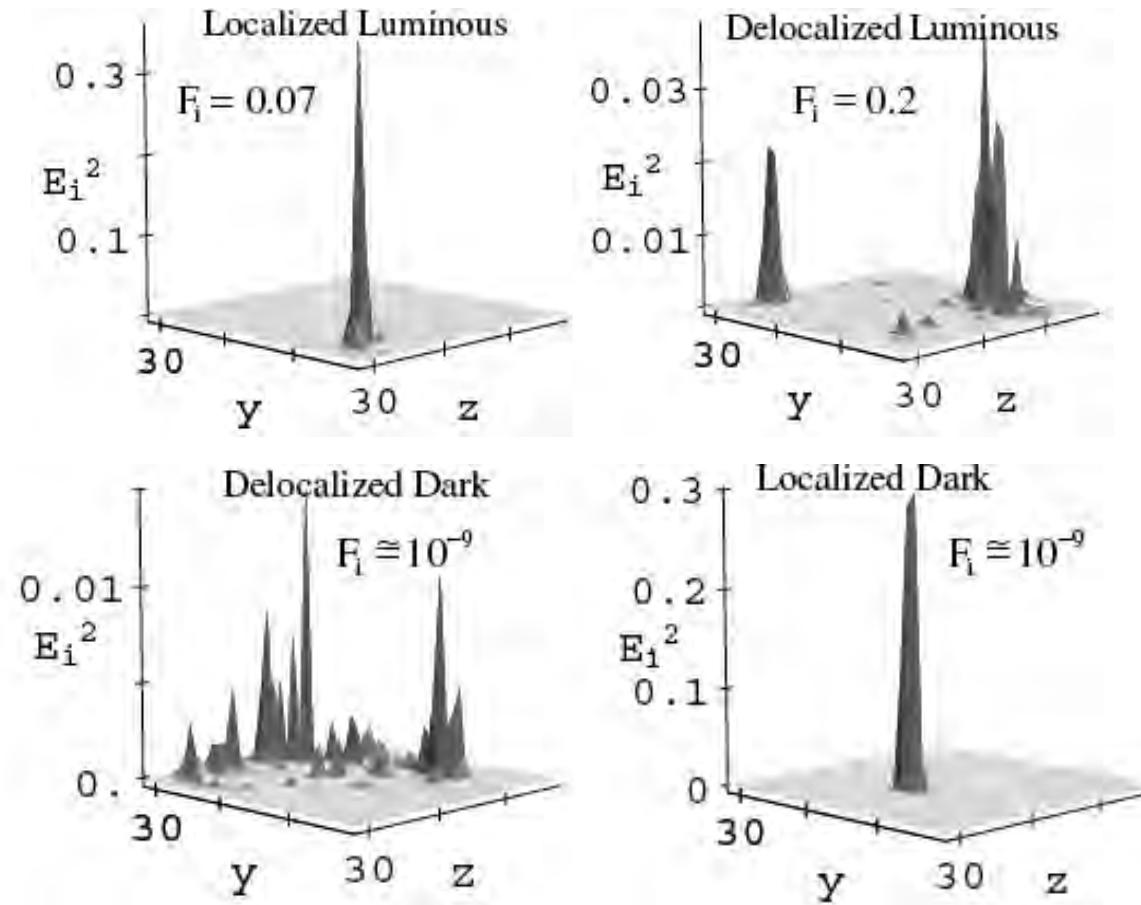


Surface (TEM image)  
Gold on glass substrate



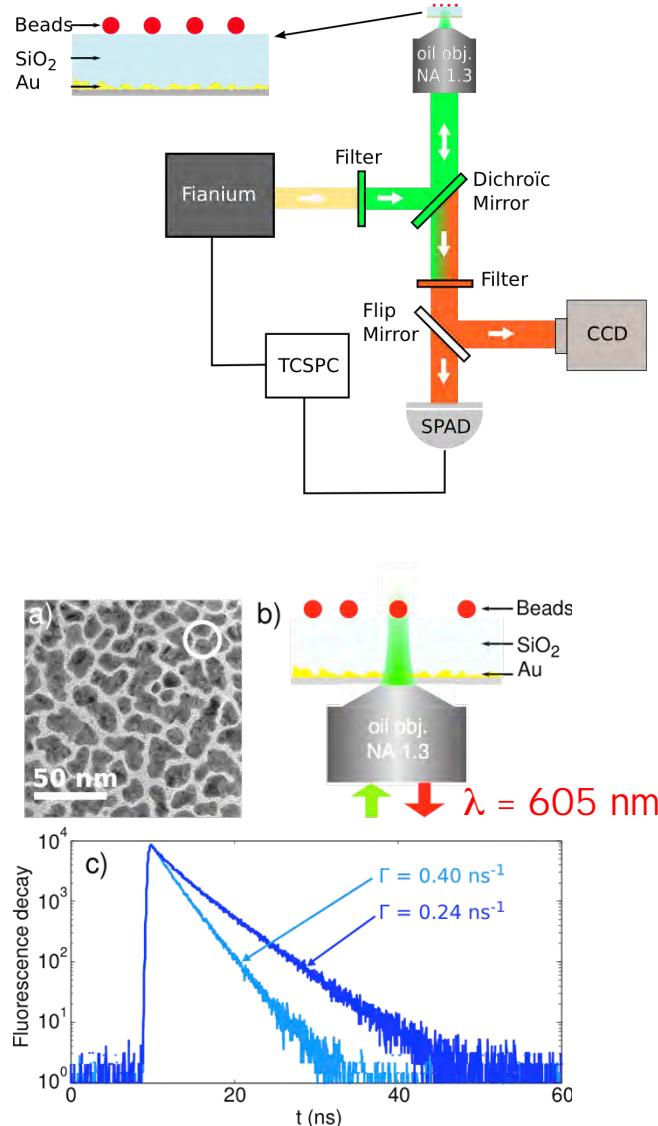
# Localized and delocalized modes

Hot-spots modes on a fractal disordered film

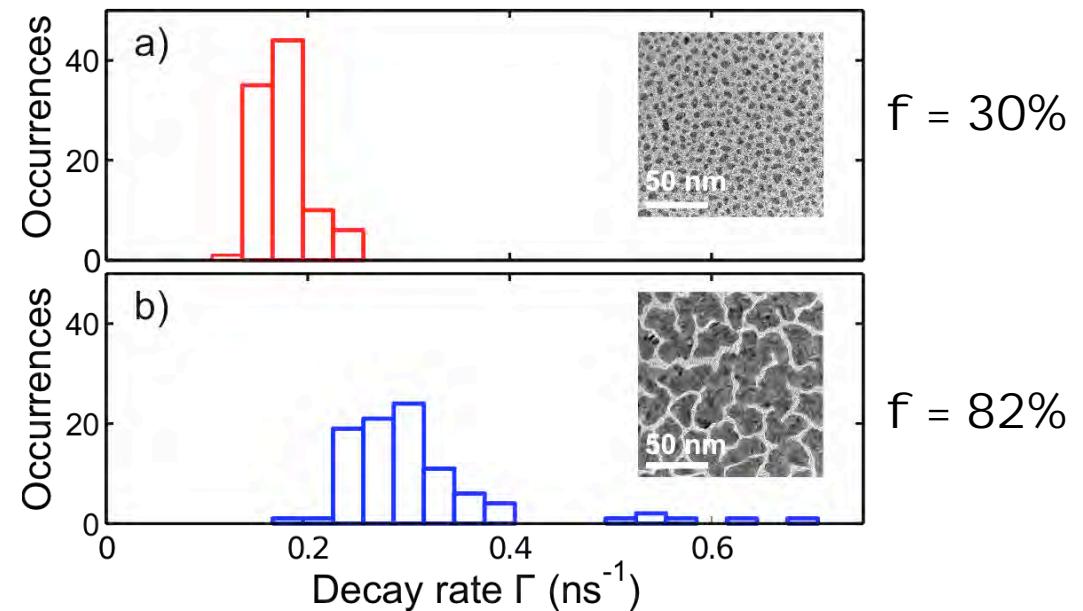


« Inhomogeneous localization »

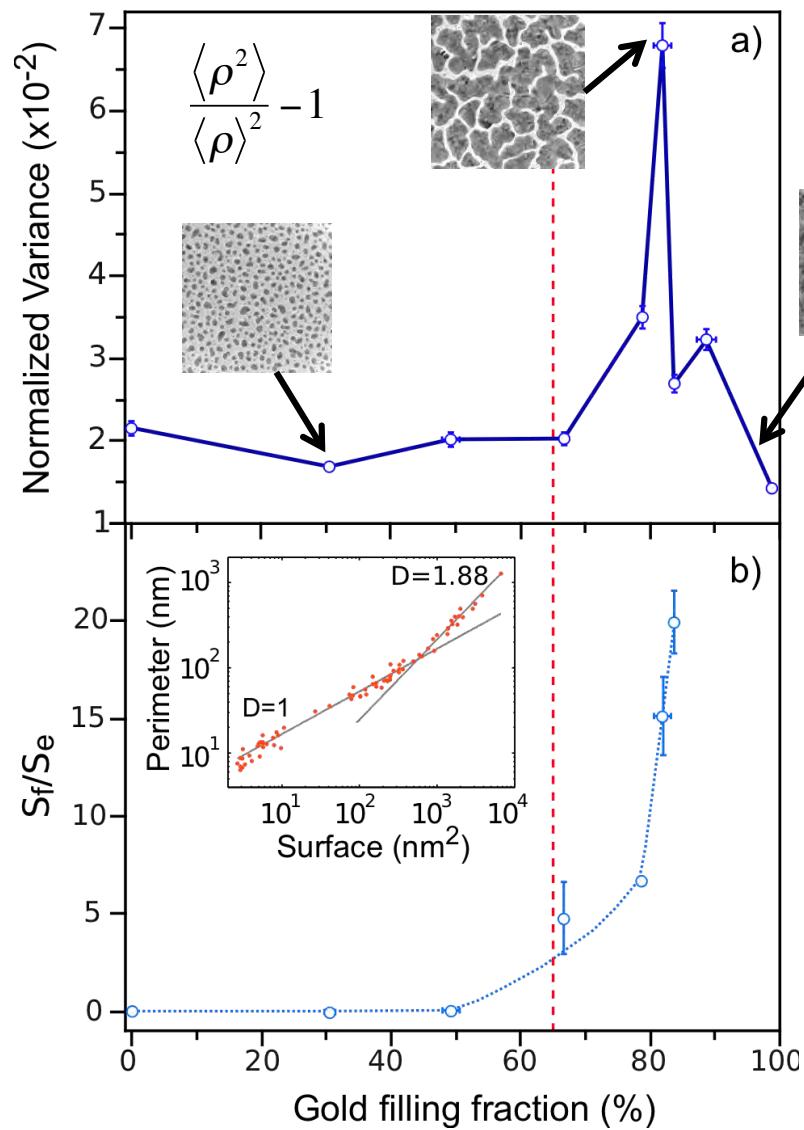
# LDOS distributions on disordered metal films



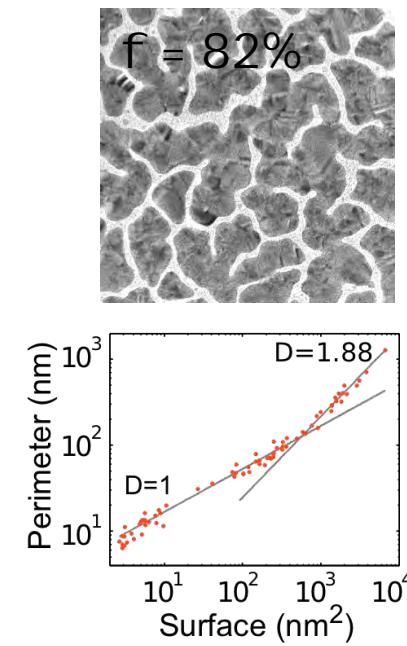
Statistical distributions of  $\Gamma$  (LDOS)



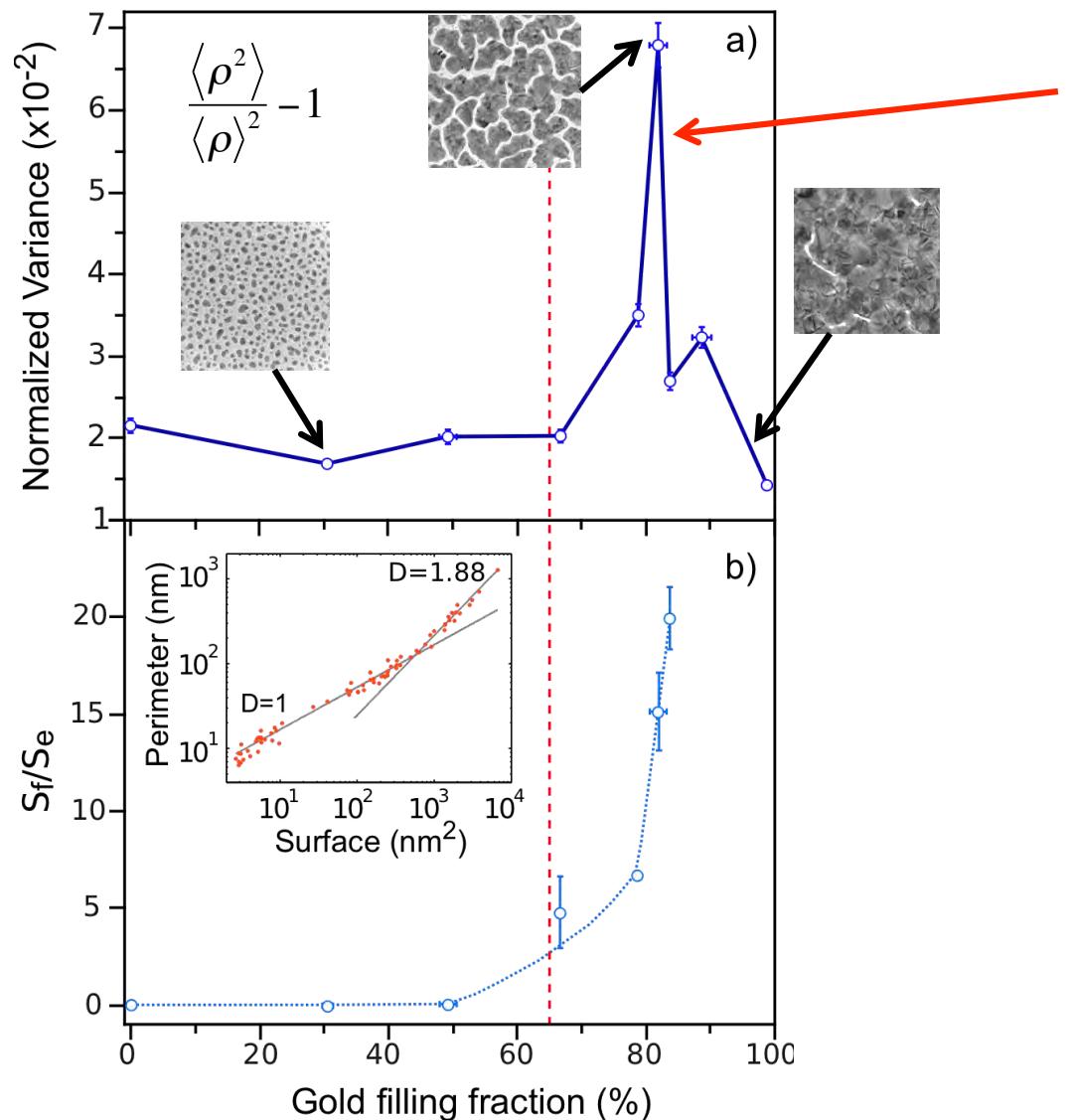
# LDOS fluctuations



Fractal and Euclidian clusters



# The peak reveals modes localization



The peak in the LDOS fluctuations is the signature of localized plasmon modes

Mode localization length  
(inverse participation ratio)

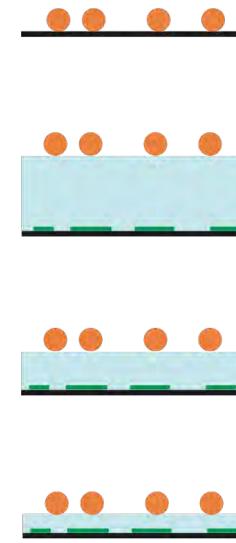
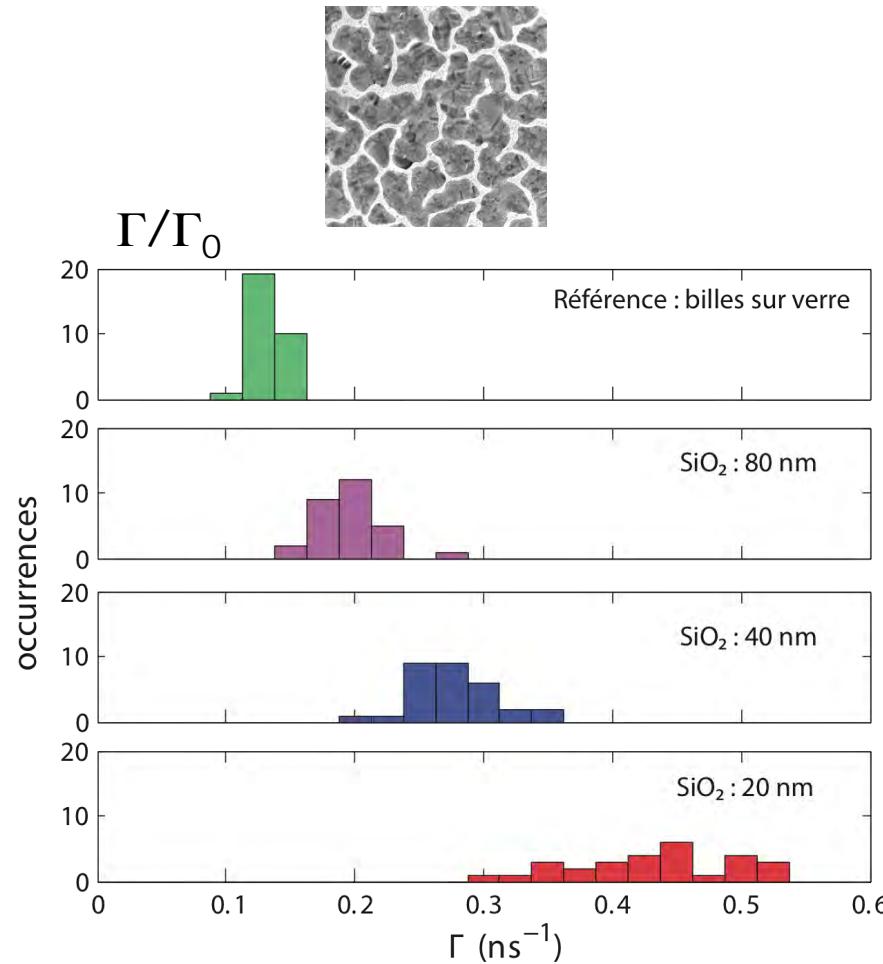
$$R_{IP} = \frac{\int |\mathbf{E}(\mathbf{r})|^4 d^2r}{\left[ \int |\mathbf{E}(\mathbf{r})|^2 d^2r \right]^2} \approx \frac{1}{\xi^2}$$

$$R_{IP} \approx \frac{1}{S} \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2}$$

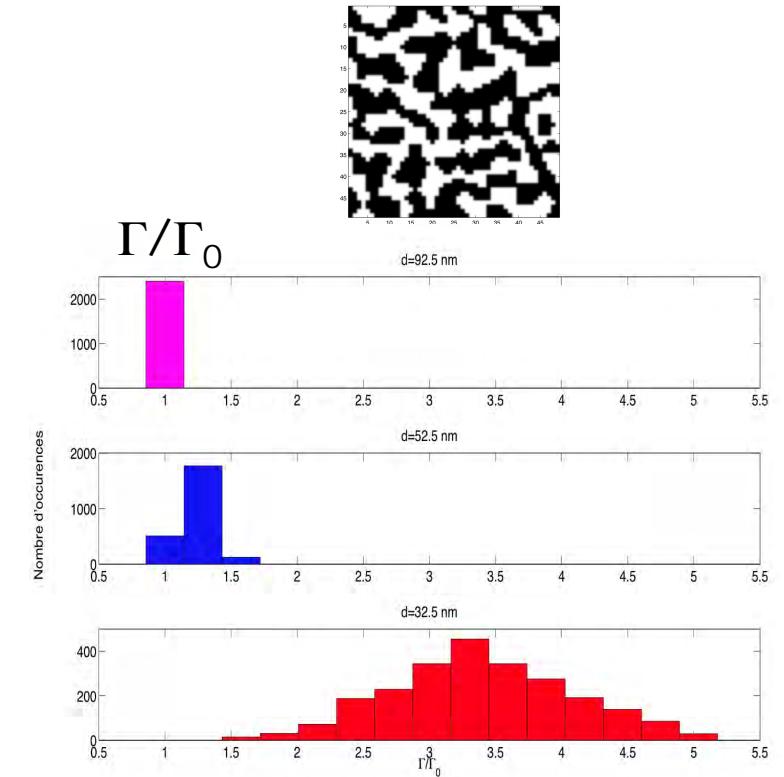
$$\boxed{\frac{1}{S} \frac{\langle \rho^2 \rangle}{\langle \rho \rangle^2} \approx \frac{1}{\xi^2}}$$

# Numerical simulations

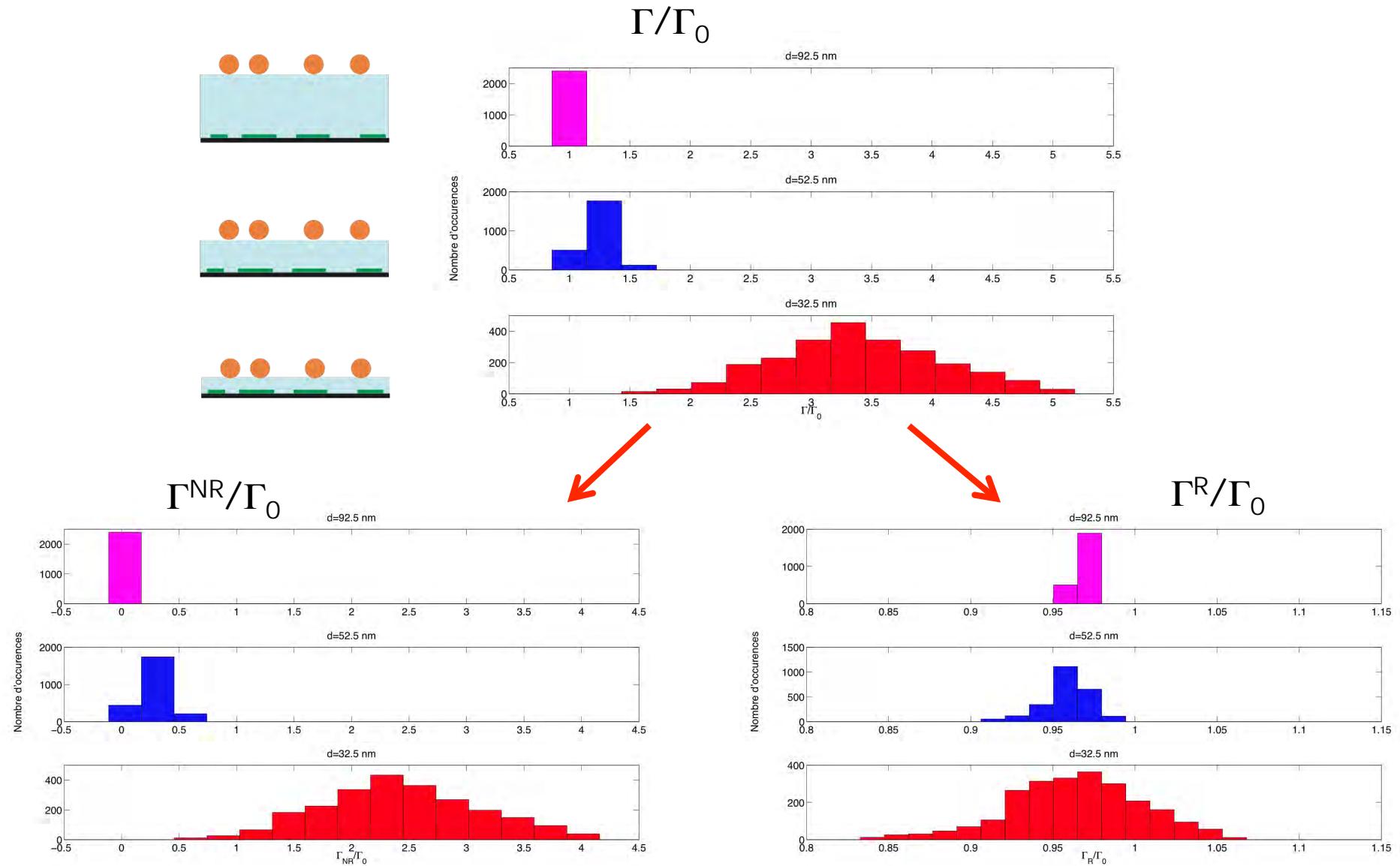
## Experiment



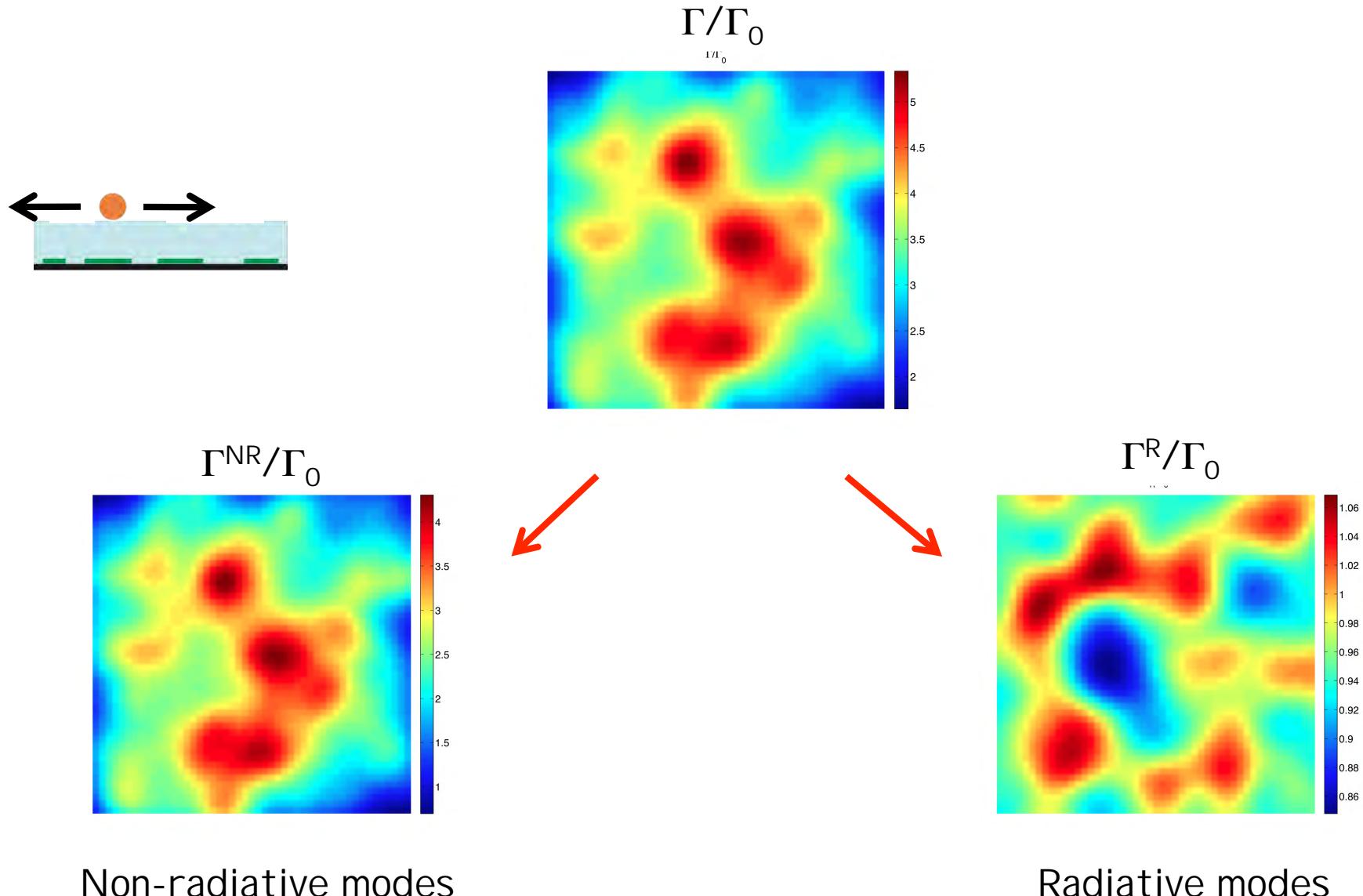
Numerical simulations  
(volume integral equation  
+ moment method)

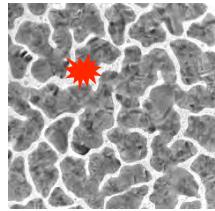


# Radiative and non-radiative decays can be separated

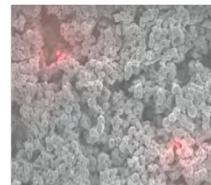


# Mapping radiative and non-radiative contributions





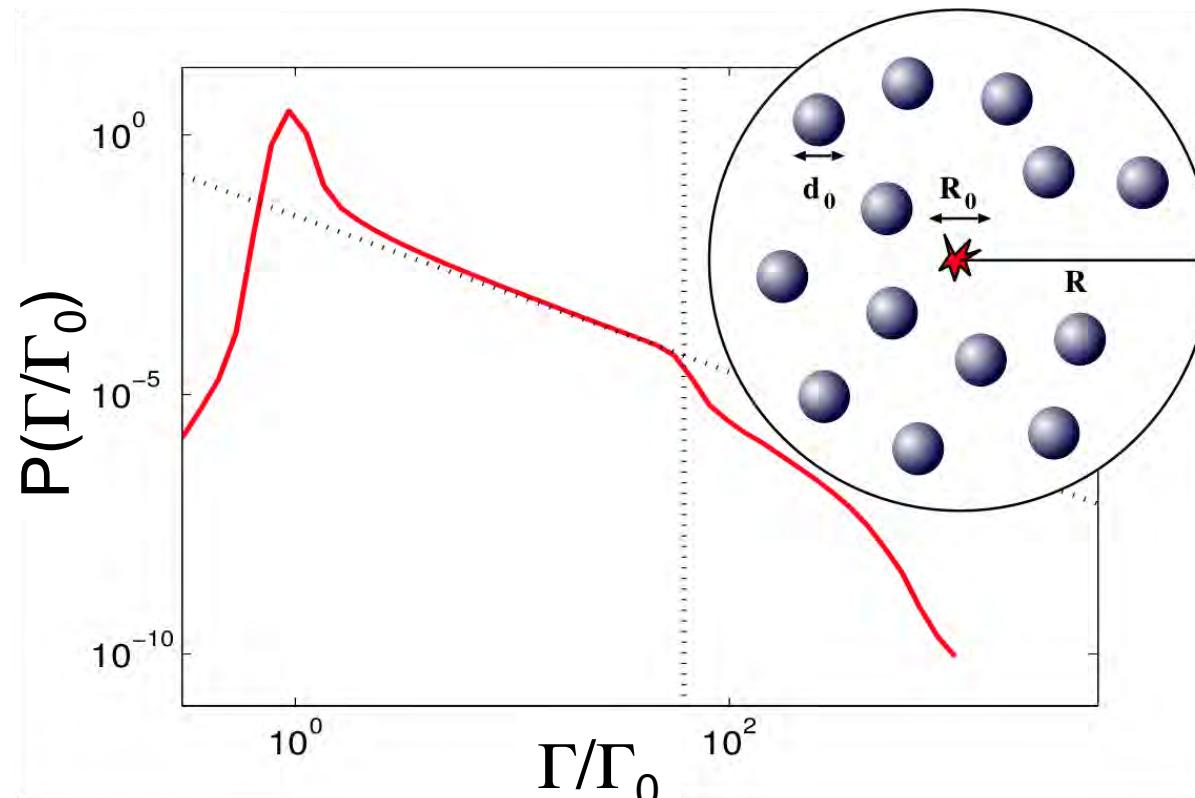
Spontaneous emission and plasmonics:  
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Probing near-field interactions in volume  
disordered systems

# LDOS statistics from « numerical experiments »

Statistical distribution of decay rate  $\Gamma$  (LDOS)



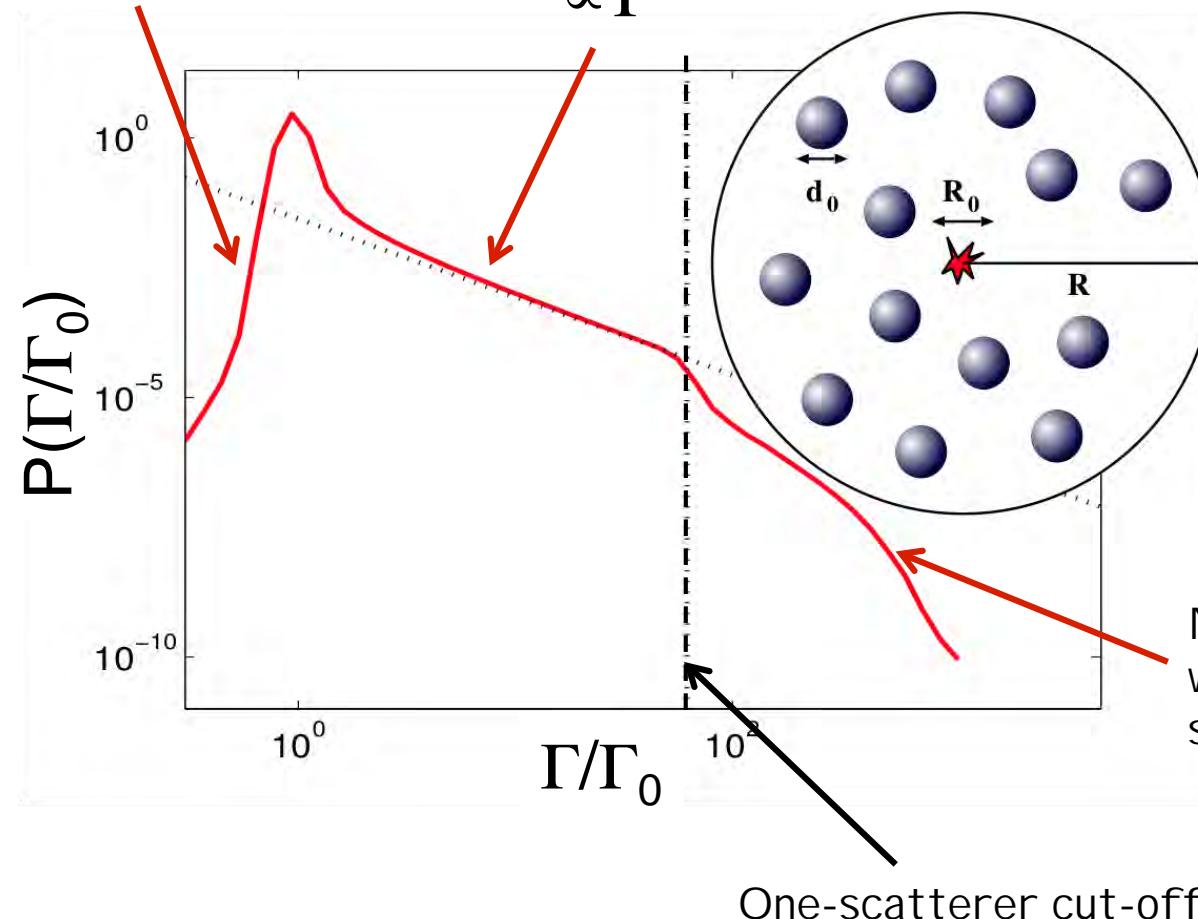
- Resonant point scatterers (« atoms »)
- $\lambda \approx 630 \text{ nm}$
- Cluster size  $R = 1.2 \mu\text{m}$
- Exclusion volume  $R_0 = 50 \text{ nm}$

# Long tail: Near-field interactions

Multiple scattering  
and collective interactions

Near-field interaction  
with one scatterer

$$\propto \Gamma^{-3/2}$$

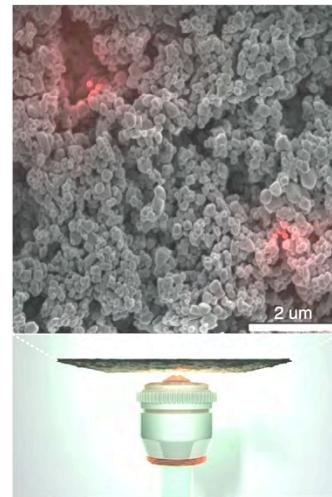


Near-field interaction  
with more than one  
scatterer

One-scatterer cut-off

# Broad - asymmetric distribution of decay rates (LDOS)

Experiments: Sapienza, Bondareff, Habert, van Hulst, ICFO (Barcelona, Spain)



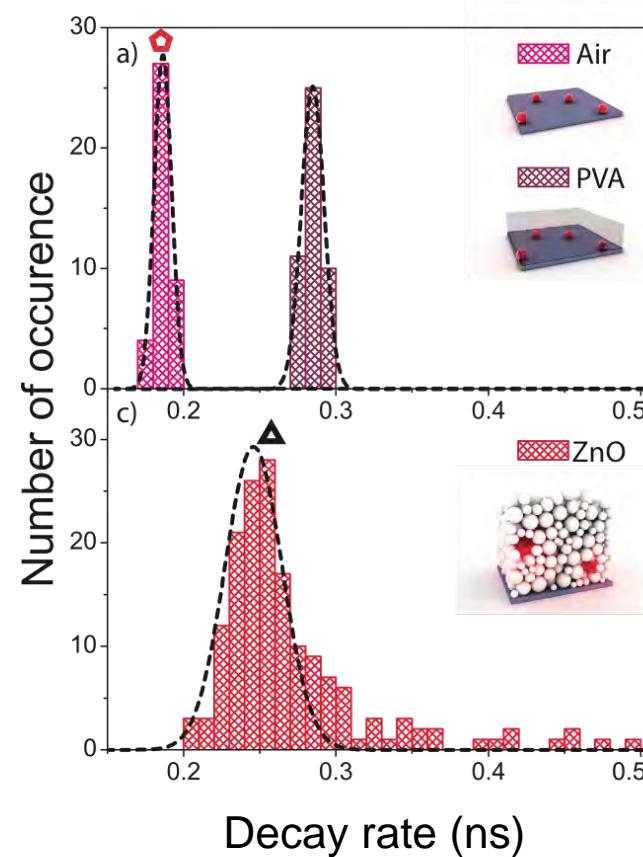
ZnO powder  
Polydisperse particles  
 $(140 \pm 50 \text{ nm})$

Photon mean free path

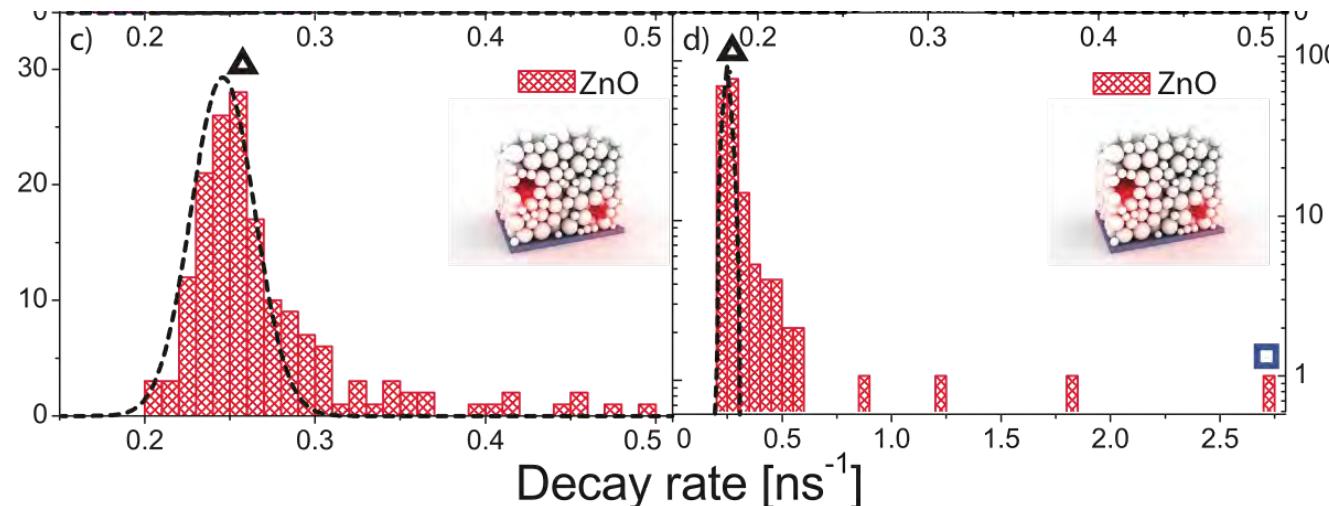
$$\ell = 0.9 \text{ } \mu\text{m}$$

$$k\ell = 9.4$$

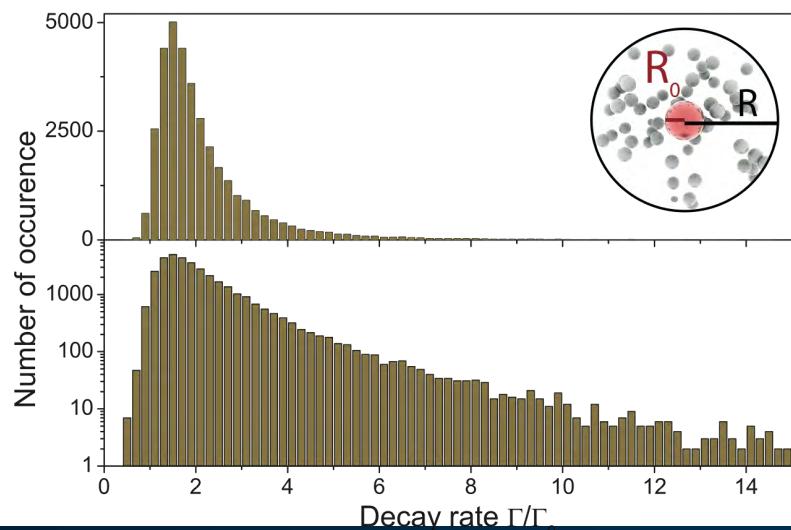
LDOS statistics probed by lifetime  
of nanosources (24 nm fluorescent beads)



# Long tail controlled by near-field interactions



Theory



- Tail results from near-field interactions
- High Purcell factors (rare events)

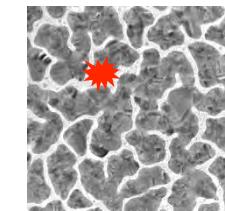
$$\frac{\Gamma_{\max}}{\Gamma_{peak}} \approx 9$$

$$\frac{\Gamma_{\max}}{\Gamma_0} \approx 15$$

# Summary

- Photonic modes in complex systems can be probed with LDOS statistics

*Evidence of spatially localized modes  
Radiative versus non-radiative decay*



- Disordered photonic materials can lead to substantial modifications of spontaneous emission

*Rare events can produce substantial changes  
Sensitive probe of nanoscale environment*

