

*Higher-order resonances in **single**-arm nanoantennas:  
Evidence of **Fano**-like interference  
FANO PLASMONICS MADE SIMPLE*

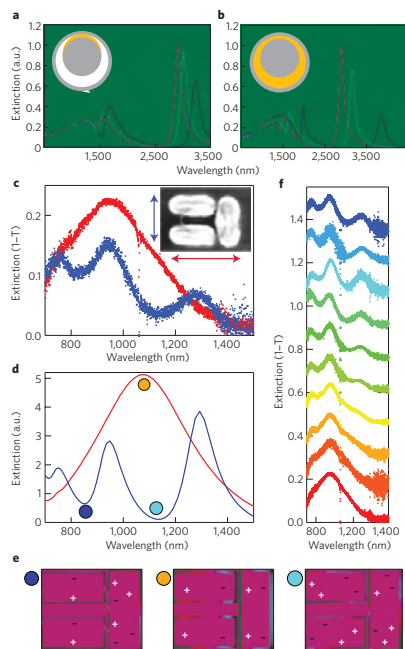
**F. López-Tejeira, R. Paniagua-Domínguez, R. Rodríguez-Oliveros**

**José A. Sánchez-Gil,**

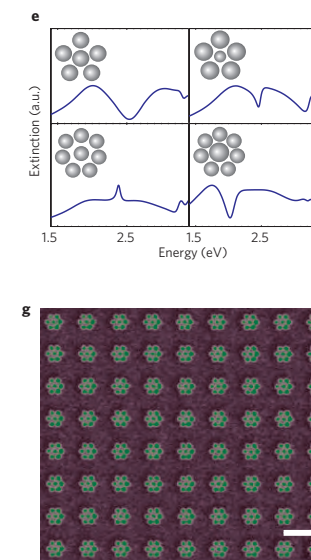
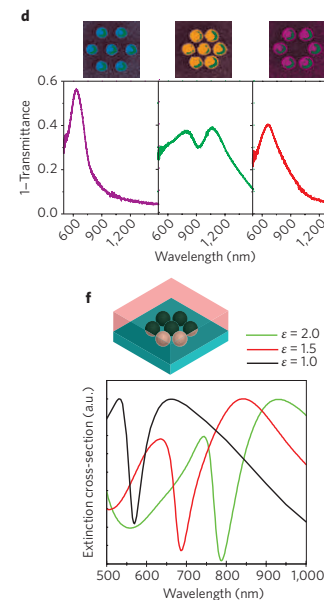
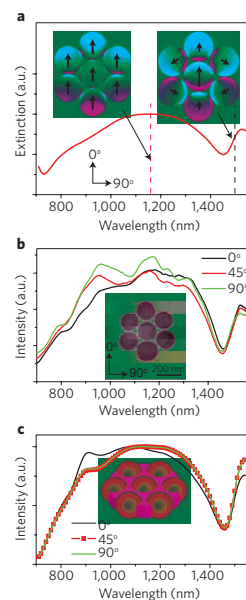
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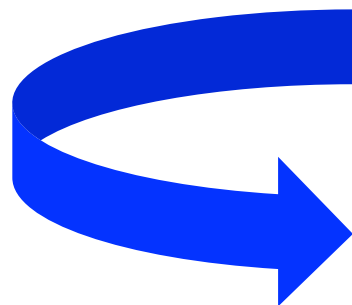
## Fano-like plasmon resonances on a variety of complex nanostructures



Nano-disk-rings,  
nanodolmens,  
nanoclusters, ...



Luk'yanchuk, Zheludev, Maier, Halas, Nordlander, Giessen, Chong, Nat. Mater. 2010

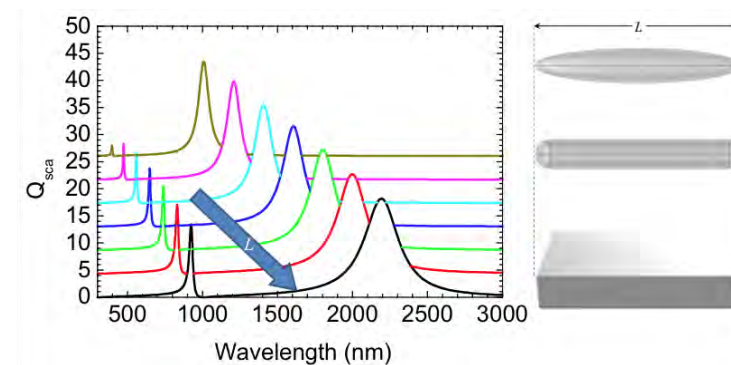




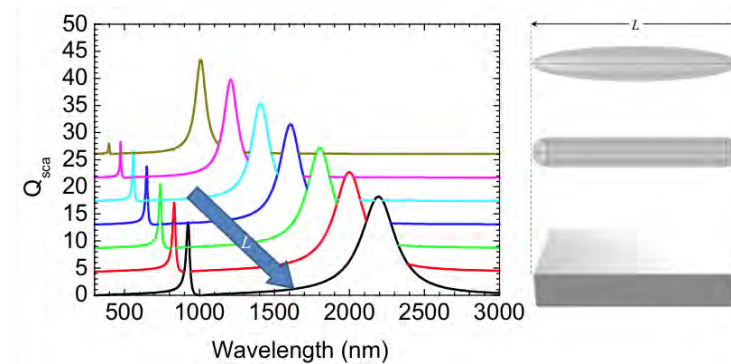


  
 ( $Q_{sca}$ ) SINGLE NANOPARTICLES

- Introduction: Plasmon Fano reso/single-NP
- Nano-Spheroid
  - Quasi-analytical approach: Mode interference
- Nano-rods & nano-wires
  - Numerical calcs
  - 1<sup>st</sup>-3<sup>rd</sup> mode: Spatial interference
- Conclusions:  
Spectral & spatial overlap



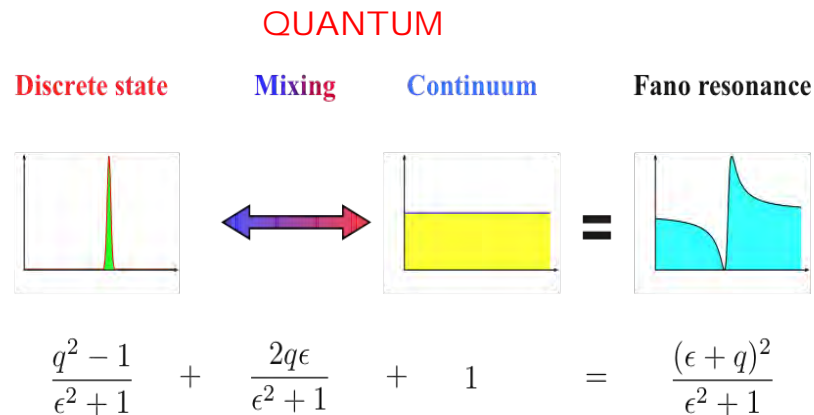
- Introduction: Plasmon Fano reso/single-NP **Why not?**
- Nano-Spheroids
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A **Fano resonance** exhibits a distinctly asymmetric shape with the following functional form:

$$\frac{(F\gamma + \omega - \omega_0)^2}{(\omega - \omega_0)^2 + \gamma^2}$$

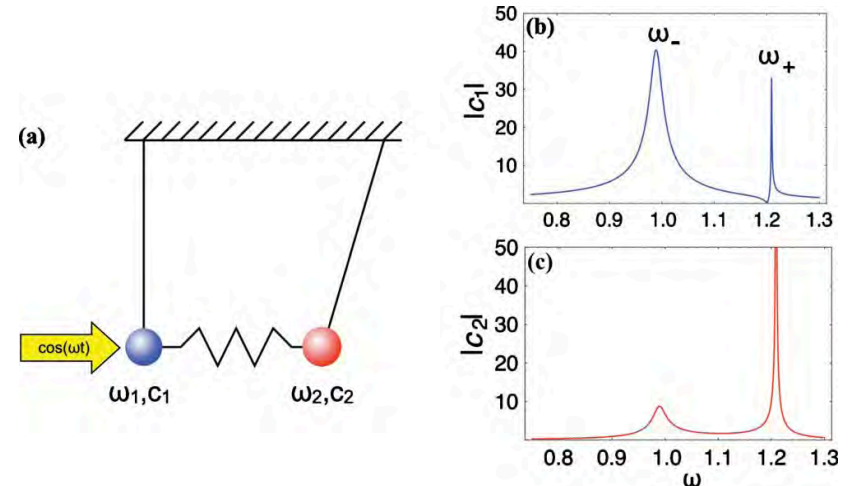
where  $\omega_0$  and  $\gamma$  are standard parameters that denote the position and width of the resonance, respectively;  $F$  is the so-called Fano parameter, which describes the degree of asymmetry. The microscopic origin of the Fano resonance arises from the constructive and destructive interference of a narrow discrete resonance with a broad spectral line or continuum.



Fano, "Effects of configuration interaction on intensities and phase shifts", Phys. Rev. 1961.

Miroshnichenko, Flach, Kivshar, Rev. Mod. Phys. 2010

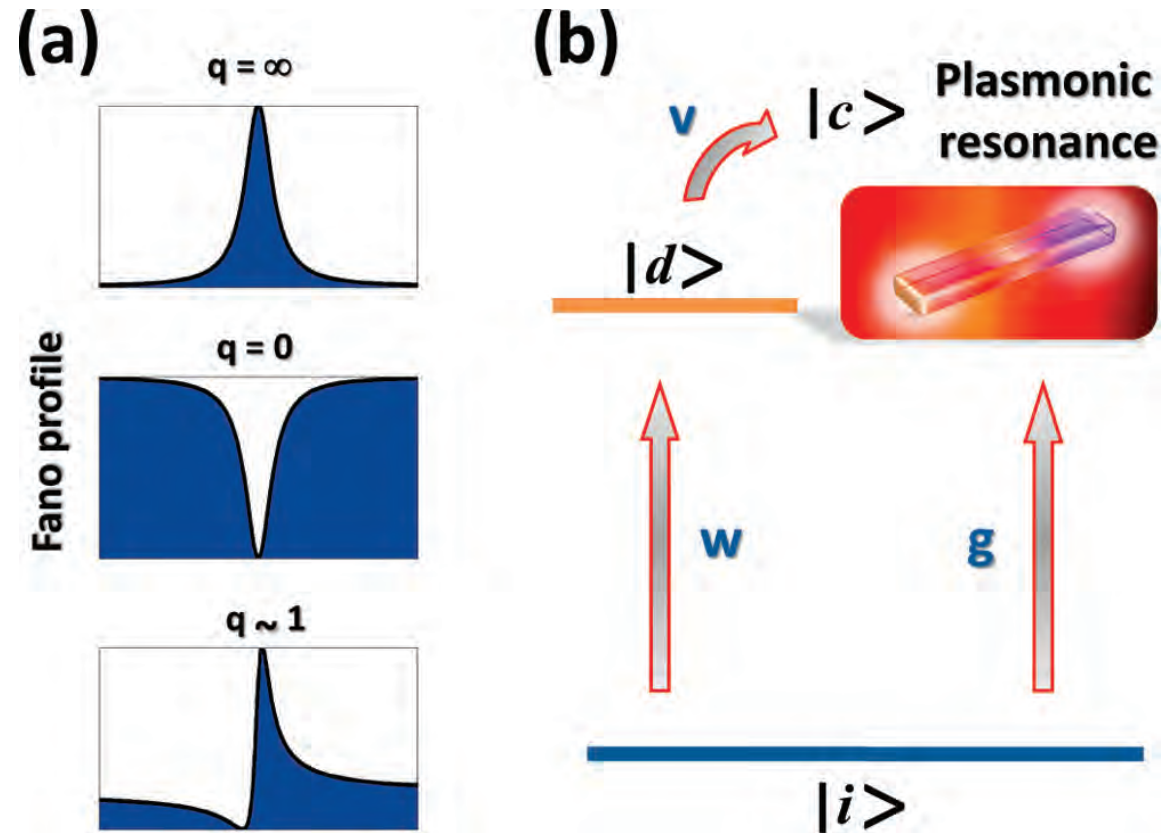
CLASSICAL



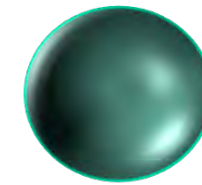
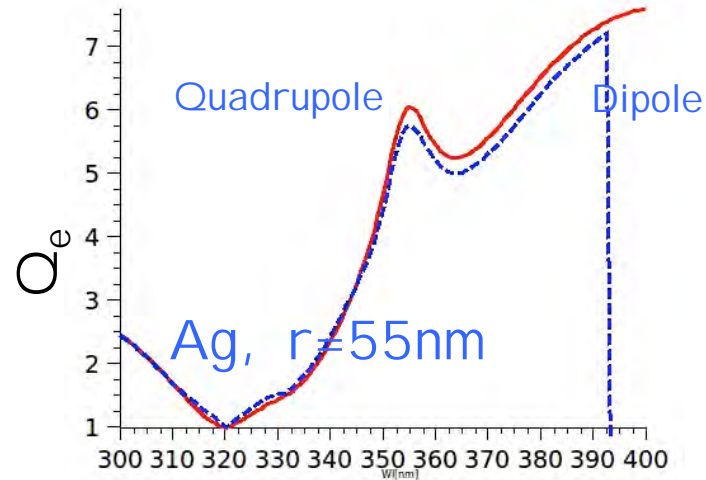
Joe, Satanin, and Kim, "Classical analogy of Fano resonances," Phys. Scr. 2006.

## Plasmon-Fano model

Giannini, Francescato, Amrania, Phillips, Maier, Nano Lett. 2011



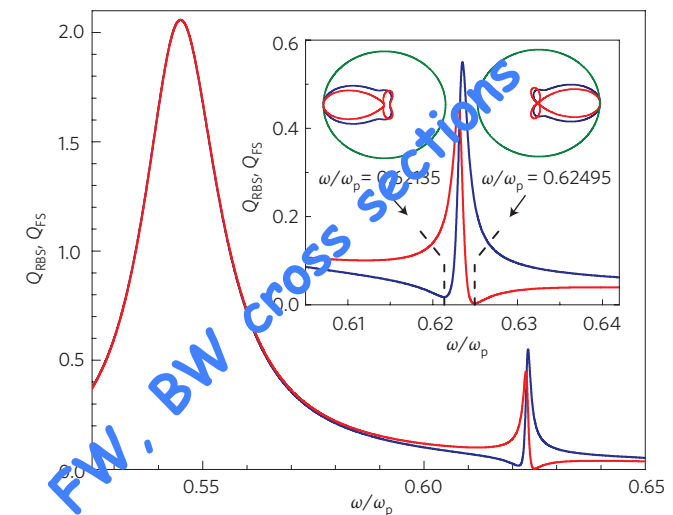
## PLASMONICS: SPHERE → Mie scattering



BROAD mode (Lowest-order, E-Dipole)  
DARK mode (Higher-order, EM Multipole)

$$Q_{sca} = \frac{2}{q^2} \sum_n (2n + 1) \left[ |a_n|^2 + |b_n|^2 \right]$$

$Q_{sca}$  Mie → NO INTERFERENCE!!



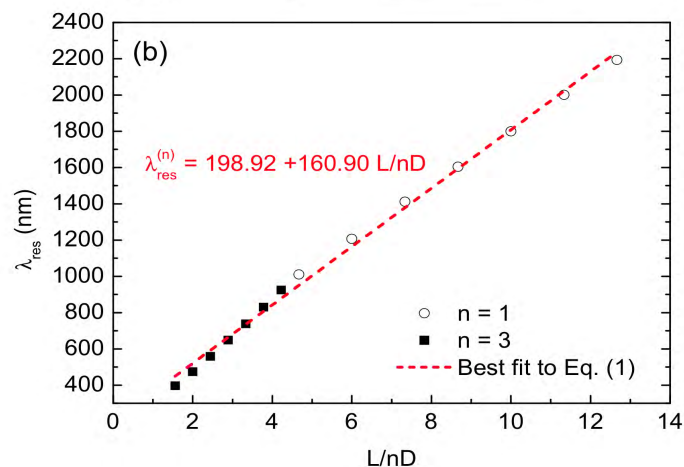
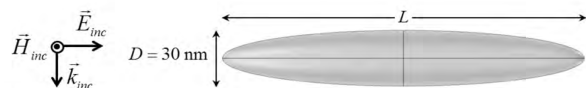
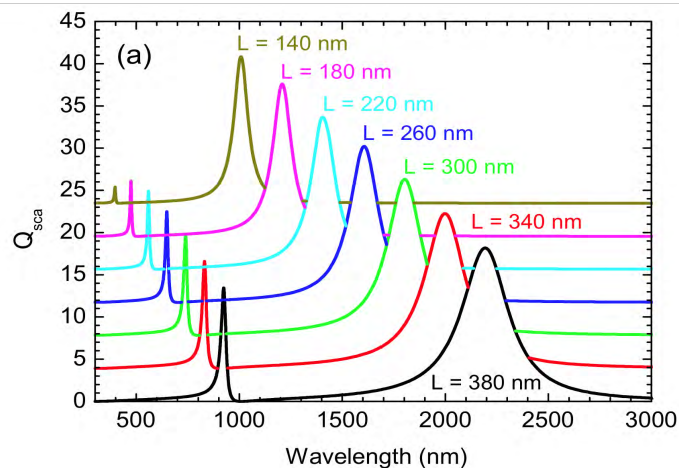
Luk'yanchuk, Zheludev, Maier, Halas, Nordlander, Giessen, Chong, Nat. Mater. 2010

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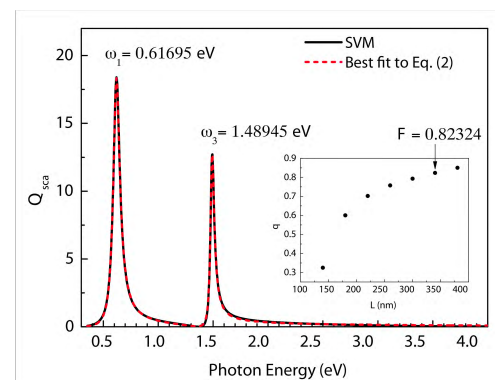
## Longitudinal plasmon resonances Separation of variables (SVM)

Normal incidence: odd-symmetry modes



## Modified Fano line shape

$$Q_{sca}(\omega) \propto \left| A(\omega) + B \left[ \frac{b_1}{(\omega - \omega_1) + ib_1} + \frac{Fb_3}{(\omega - \omega_3) + ib_3} \right] \right|^2$$

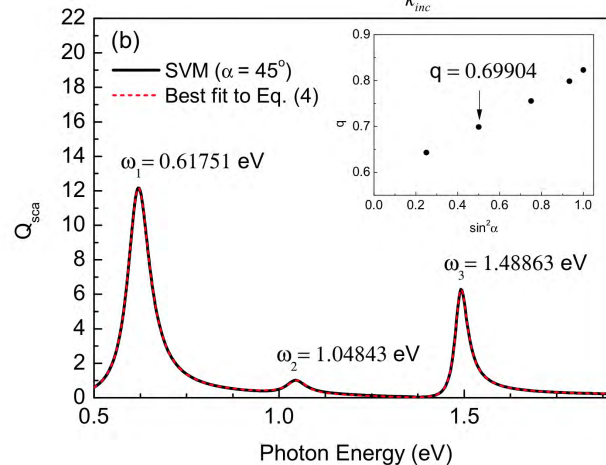
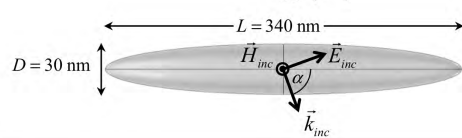
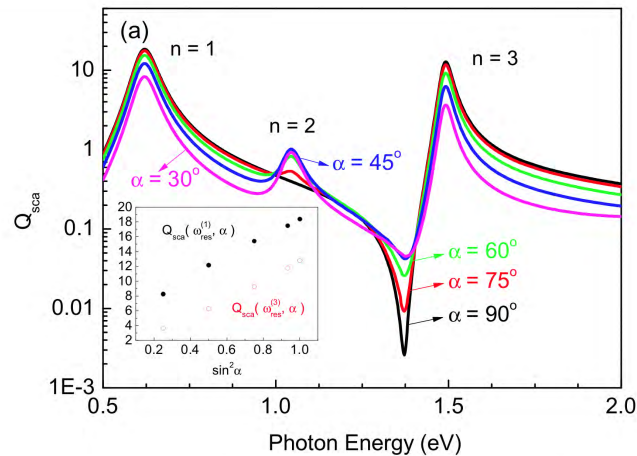


López-Tejera, Rodríguez-Oliveros, Paniagua-Domínguez, Sánchez-Gil, preprint

## Longitudinal plasmon resonances

Oblique incidence: all modes  $n=1,2,3,\dots$

SVM



Fano line-shape + Lorentzian  
 $N=1,3$  +  $N=2$



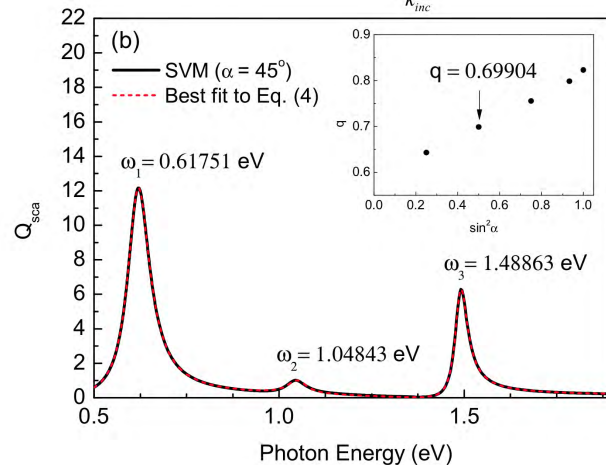
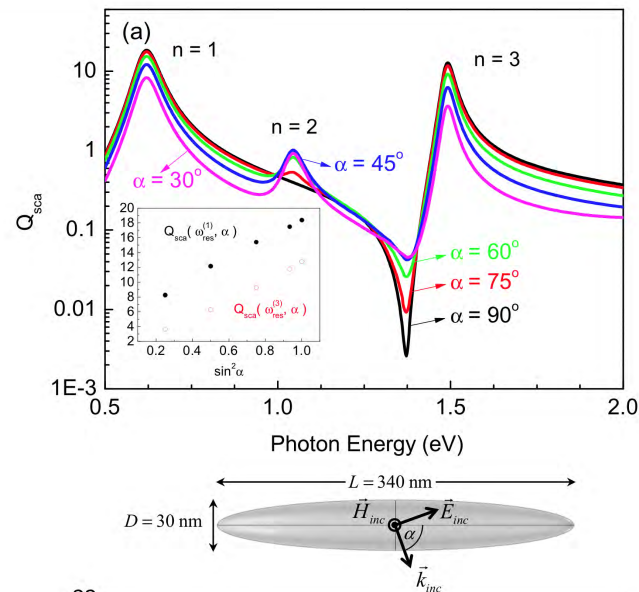
$$Q_{sca}(\omega, \alpha \neq 90^\circ) \approx |f(\omega)|^2 + \frac{|B_2|^2 b_2^2}{b_2^2 + (\omega - \omega_2)^2}$$

López-Tejiera, Rodríguez-Oliveros, Paniagua-Domínguez, Sánchez-Gil, preprint

## Longitudinal plasmon resonances

Oblique incidence: all modes  $n=1,2,3,\dots$

## Separation of variables (SVM) ~ Extended Mie



$$\mathcal{Q}_{sca} = \frac{4}{LDk_d^2} \left\{ 2 \sum_{l=1}^{\infty} |b_l^{(1)}|^2 N_{1l}^2(c_d) + \text{Re} \sum_{l=1}^{\infty} \sum_{m=l}^{\infty} \sum_{n=m}^{\infty} i^{n-l} \left[ k_d^2 a_{ml}^{(d)} (a_{mn}^{(d)})^* \omega_{ln}^{(m)}(c_d, c_d) + ik_d \left( b_{ml}^{(d)} (a_{mn}^{(d)})^* \kappa_{ln}^{(m)}(c_d, c_d) - a_{ml}^{(d)} (b_{mn}^{(d)})^* \kappa_{nl}^{(m)}(c_d, c_d) \right) + b_{ml}^{(d)} (b_{mn}^{(d)})^* \tau_{ln}^{(m)}(c_d, c_d) \right] N_{ml}(c_d) N_{mn}(c_d) \right\}$$



Mie-like: NO INTERFERENCE

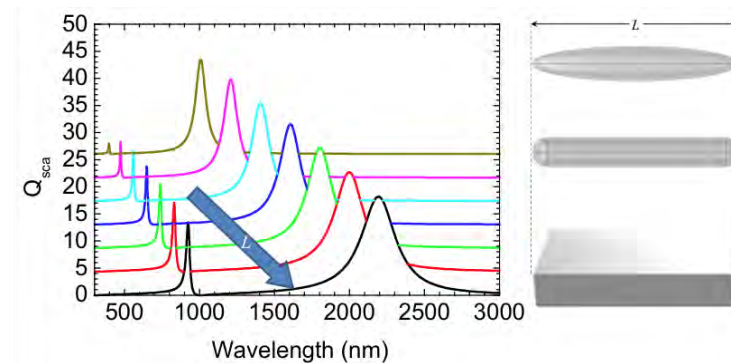


Ext-Mie: INTERFERENCE

López-Tejiera, Rodríguez-Oliveros, Paniagua-Domínguez, Sánchez-Gil, preprint

- Plasmon Fano reso/**single-Nano-Spheroids**
- Quasi-analytical approach: Mode interference
- Odd modes: 1<sup>st</sup>-3<sup>rd</sup> interference
- Even-odd modes: 1<sup>st</sup>-2<sup>nd</sup> NO interference
- Explore other single NP geometries

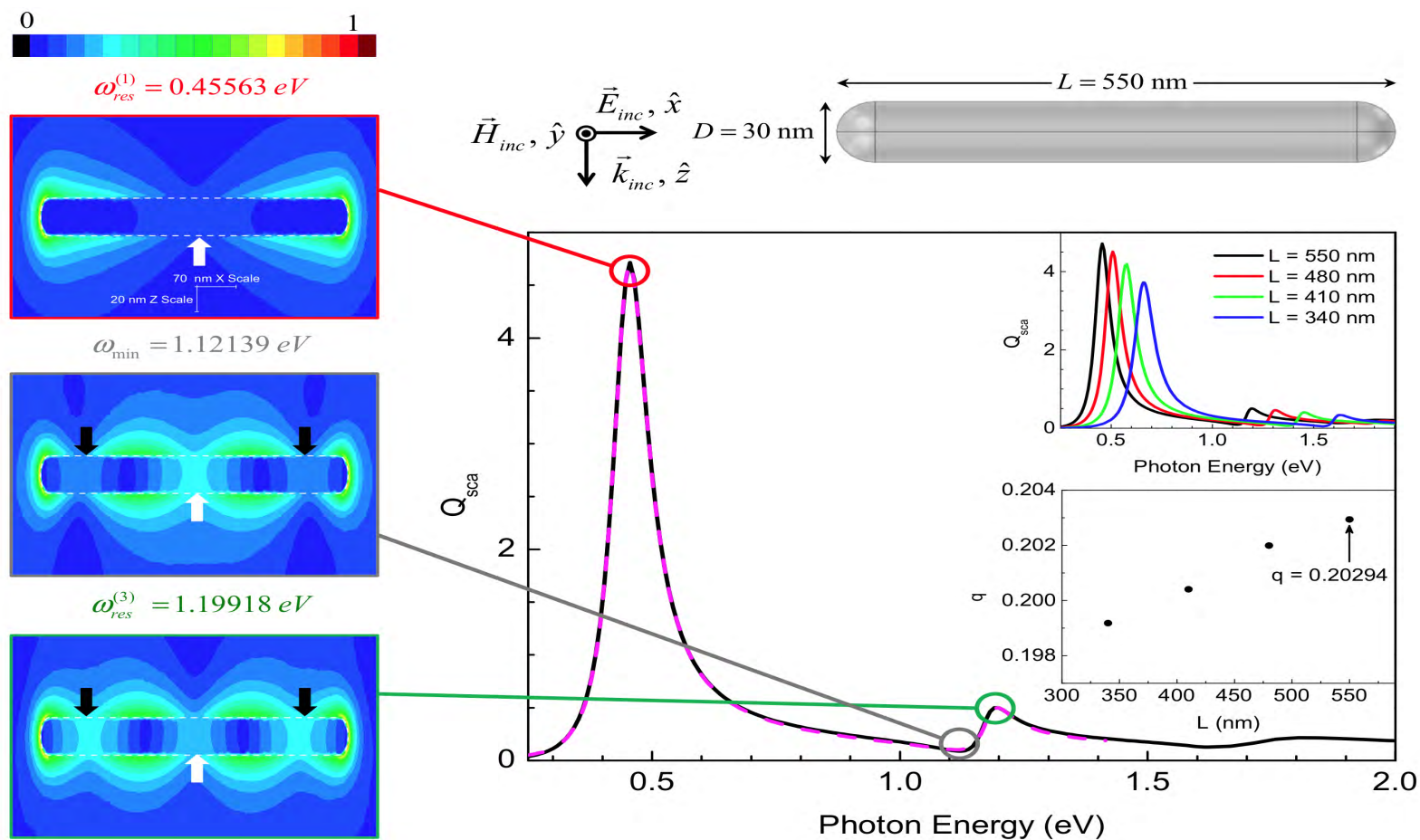
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## Longitudinal $L \sim n\lambda/2$ resonances

Oblique incidence: all modes  $n=1,2,3,\dots$

## FEM-COMSOL



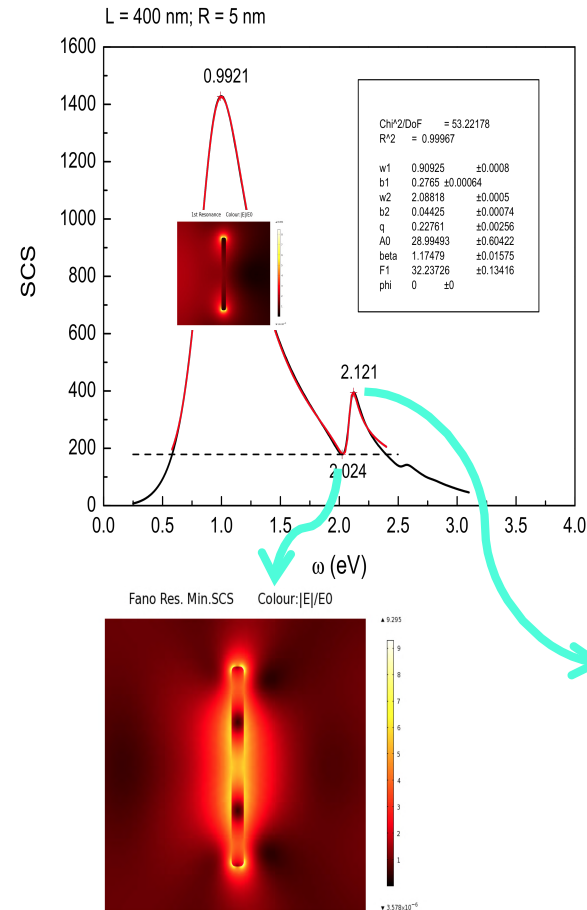
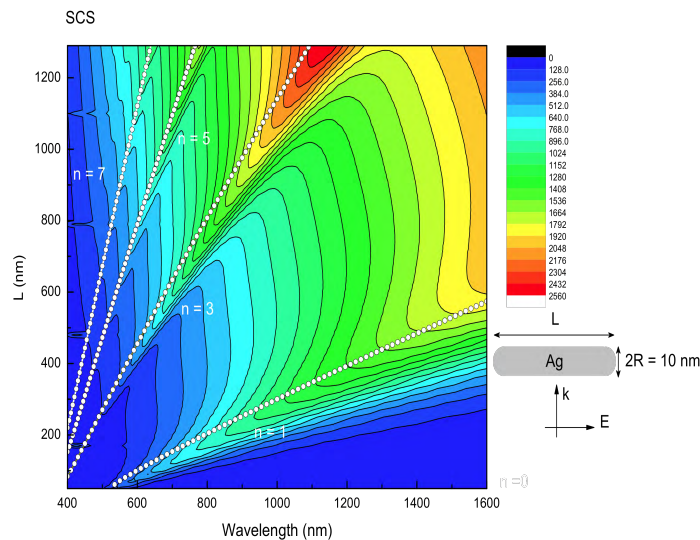
Nanowire (~2D Nanorods)

Longitudinal  $L = n\lambda_{\text{eff}}/2[1-R]$  resonances

Normal incidence: odd modes

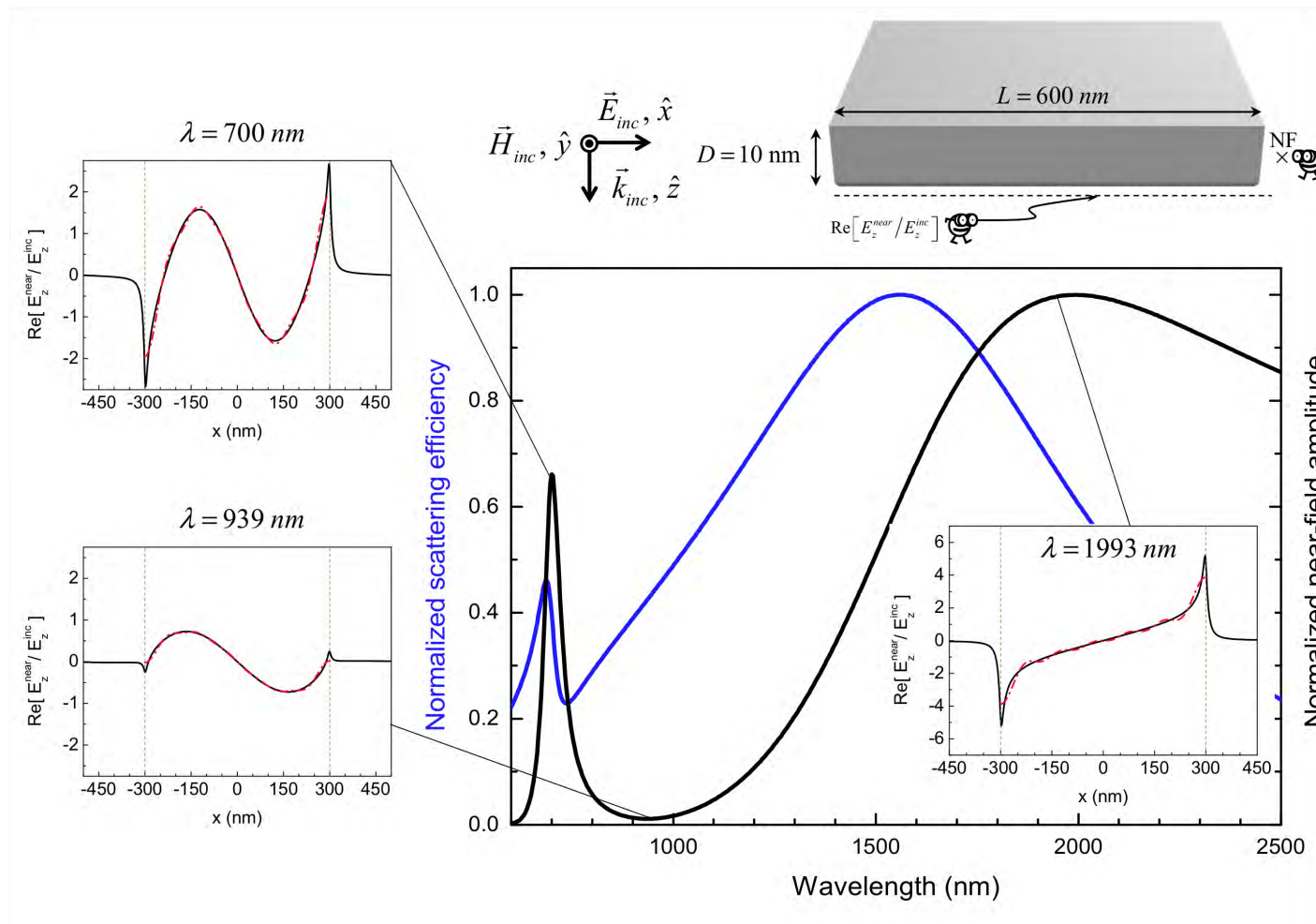
$n=1$  (HW) ▶ Broad, Bright  
 $n=3,5,\dots$  (HW) ▶ Narrow, Dark

2DSIE



Modified Fano line-shape fit

## Spatial Mode Interference



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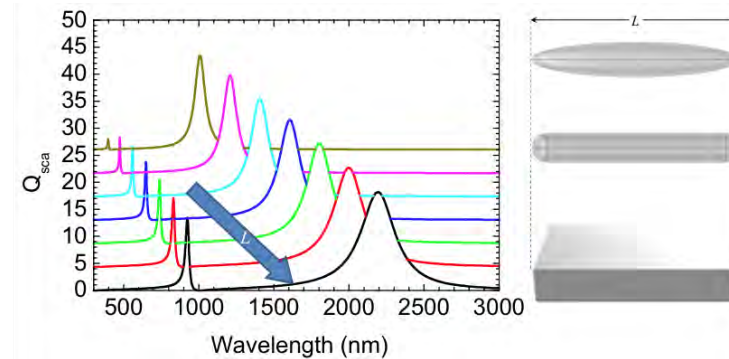


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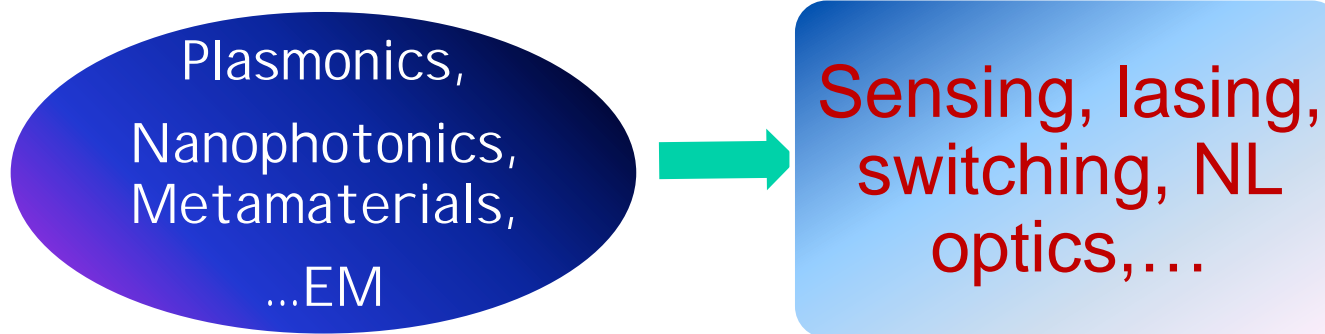
► Fano-like LSPR on a single nanorod

► Spectral & Spatial overlap

Explore new physics & configurations



► Applications: Fano made simple!!



## Coworkers

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**Rogelio Rodríguez-Oliveros**

**Ramón Paniagua-Domínguez**



**Fernando López-Tejeira**



## Funding agencies





IEM



*...Thank you*