## Linear Shear Elasticity and Osmotic Pressure of Concentrated Disordered Ionic Emulsions

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## **Abstract**

We present a free energy model that describes two key thermodynamic properties, the osmotic pressure  $\Pi$  and the linear elastic shear modulus  $G_p'$  of a disordered system of concentrated deformable emulsion droplets stabilized by ionic surfactants over a range of volume fractions below, near, and above the random jamming point  $\phi_c$ . The model unifies existing approaches 1.2.3 by considering entropic, electrostatic, and interfacial (EEI) contributions to a free energy, which depends on the droplet volume fraction  $\phi$  and the applied shear strain  $\gamma$ . This EEI free energy is minimized with respect to an average deformation parameter that links these three contributions. This minimization reveals that the entropic term is dominant for  $\phi$  well below  $\phi_c$ , the electrostatic term is dominant for  $\phi$  below  $\phi_c$ , and the interfacial term is dominant for  $\phi$  above  $\phi_c$ . The predictions of the model describe measurements of  $G_p'(\phi)^{4.5}$  for colloidal emulsions ranging from nanoscale to microscale, and also measurements of  $\Pi(\phi)$  for microscale emulsions. Although emulsions stabilized by ionic surfactants that have been concentrated into disordered structures are technically out-of-equilibrium systems, this near-equilibrium minimization approach nevertheless reasonably predicts the constitutive properties of these systems.

## References

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